

BCM SCHOOL, BASANT AVENUE, DUGRI ROAD, LUDHIANA
Class XII (Continuity and differentiability)

Sol 1.	(a)
2.	(c)
3.	(d)
4.	Take log on both sides, $\log x = \frac{x}{y} \Rightarrow y = \frac{x}{\log x}$ Now differentiate both sides to get $\frac{dy}{dx} = \frac{\log x - 1}{(\log x)^2}$.
5.	At $x = 3$, LHL = RHL $3a + 1 = 3b + 3 \Rightarrow a - b = 2/3$
6.	Let $u = \tan^{-1} \left[\frac{\sqrt{1+x^2}-1}{x} \right]$ By substituting $x = \tan \theta$, $u = \frac{1}{2} \tan^{-1} x$ So, $\frac{du}{dx} = \frac{1}{2} \cdot \frac{1}{1+x^2}$ Also, let $v = \tan^{-1} x$ $\frac{dv}{dx} = \frac{1}{1+x^2}$ So, $\frac{du}{dv} = \frac{1}{2}$
7.	Taking log on both sides, $16 \log x + 9 \log y = 17 \log (x^2 + y)$ Differentiate both sides and simplify to get $\frac{dy}{dx} = \frac{2y}{x}$
8.	On differentiating both sides, we have $(x + y \frac{dy}{dx}) \left(\frac{2}{x^2+y^2} \right) = \frac{2}{x^2+y^2} (x \frac{dy}{dx} - y)$ $\frac{dy}{dx} = \frac{-(x+y)}{x-y}$
9.	$y = \sin^{-1} \left(\frac{2x}{1+x^2} \right) + \sec^{-1} \left(\frac{1+x^2}{1-x^2} \right)$, $y = \sin^{-1} \left(\frac{2x}{1+x^2} \right) + \cos^{-1} \left(\frac{1-x^2}{1+x^2} \right)$, Put $x = \tan \theta \Rightarrow \theta = \tan^{-1} x$ $y = 4\theta = 4 \tan^{-1} x$ So, $\frac{dy}{dx} = \frac{4}{1+x^2}$
10.	(i) $\frac{dy}{dx} = \frac{-(3x^2+2xy+y^2)}{x^2+2xy+3y^2}$ (ii) Taking log on both sides, $y = \frac{x}{1+\log x} \Rightarrow \frac{dy}{dx} = \frac{\log x}{(1+\log x)^2}$ (iii) $\sin y = \log x + \log y$ $\frac{dy}{dx} = \frac{y}{x(y \cos y - 1)}$ OR $y = (\sin x)^y \Rightarrow \log y = y \log(\sin x)$ $\frac{dy}{dx} = \frac{y^2 \cot x}{1 - y \cdot \log(\sin x)}$