

ANSWER KEY of class XII VECTORS	
1	$\frac{\pi}{4}$
2	8
3	$\theta = 60$
4	$5\sqrt{2}$
5	$\theta = \cos^{-1}\left(\frac{-17}{\sqrt{565}}\right)$
6	<p>Let $\vec{c} = x\hat{i} + y\hat{j} + z\hat{k}$ And $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ and $\vec{b} = \hat{j} - \hat{k}$ For $\vec{a} \times \vec{c} = \vec{b}$,</p> $\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 1 \\ x & y & z \end{vmatrix} = \hat{j} - \hat{k}$ $\Rightarrow \hat{i}(z - y) - \hat{j}(z - x) + \hat{k}(y - x) = \hat{j} - \hat{k}$ $\therefore z - y = 0 \dots(i)$ $x - z = 1 \dots(ii)$ $x - y = 1 \dots(iii)$ Also, $\vec{a} \cdot \vec{c} = 3$ $(\hat{i} + \hat{j} + \hat{k}) \cdot (x\hat{i} + y\hat{j} + z\hat{k}) = 3$ $\Rightarrow x + y + z = 3 \dots(iv)$ On adding Eqs. (ii) and (iii), we get $2x - y - z = 2 \dots(v)$ On solving Eqs. (iv) and (v), we get $x = \frac{5}{3}$ $\therefore y = \frac{5}{3} - 1 = \frac{2}{3} \text{ and } z = \frac{2}{3}$ Now, $\vec{c} = \frac{5}{3}\hat{i} + \frac{2}{3}\hat{j} + \frac{2}{3}\hat{k}$ $= \frac{1}{3}(5\hat{i} + 2\hat{j} + 2\hat{k})$

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Given

$$a \cdot b = 0 = a \cdot c$$

Thus, a is perpendicular to b and c .

A unit vector perpendicular to b and c

$$= \pm \frac{\mathbf{b} \times \mathbf{c}}{\|\mathbf{b} \times \mathbf{c}\|}$$

$$= \pm \frac{\mathbf{b} \times \mathbf{c}}{\|\mathbf{b}\|\|\mathbf{c}\|\sin\left(\frac{\pi}{6}\right)}$$

$$= \pm \frac{\mathbf{b} \times \mathbf{c}}{1/2}$$

$$= \pm 2(\mathbf{b} \times \mathbf{c}).$$