

BCM SCHOOL, BASANT AVENUE, DUGRI, LUDHIANA.

OCTOBER ASSIGNMENT- ANSWER KEY

CLASS- X (MATHEMATICS)

TOPICS: CIRCLES, AREA RELATED TO CIRCLES & SURFACE AREA AND VOLUME.

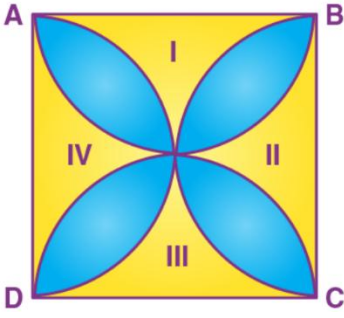
SECTION –A (MULTIPLE CHOICE QUESTIONS)

1.	(d) $3\sqrt{3}$ cm
2.	(a) 21 cm
3.	(c) 500

SECTION – B(2 MARKS QUESTIONS)

4.	$2AP = \text{Perimeter of } \Delta$ $2AP = 5 + 6 + 4 = 15 \text{ cm}$ $AP = 15/2 = 7.5 \text{ cm}$
5.	<p>The volume of water flows in the canal in one hour = width of the canal \times depth of the canal \times speed of the canal water = $3 \times 1.2 \times 20 \times 1000 \text{ m}^3 = 72000 \text{ m}^3$</p> <p>In 20 minutes the volume of water = $(72000 \times 20)/60 = 24000 \text{ m}^3$</p> <p>Area irrigated in 20 minutes, if 8 cm, i.e., 0.08 m standing water is required</p> $= 24000/0.08 = 300000 \text{ m}^2 = 30 \text{ hectares}$

SECTION – C (3 MARKS QUESTIONS)

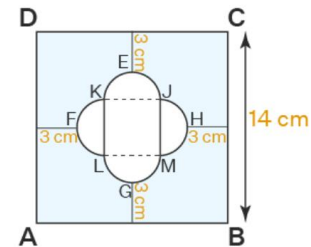
6.	<p>We have, Semi Perimeter = s Perimeter = 2s $2s = AB + BC + AC \dots [1]$ As we know, Tangents drawn from an external point to a circle are equal So we have $AF = AE \dots [2]$ [Tangents from point A] $BF = BD \dots [3]$ [Tangents From point B] $CD = CE \dots [4]$ [Tangents From point C] Adding [2], [3], and [4], $AF + BF + CD = AE + BD + CE$ $AB + CD = AC + BD$ Adding BD both side, $AB + CD + BD = AC + BD + BD$ $AB + BC - AC = 2BD$ $AB + BC + AC - AC - AC = 2BD$ $2s - 2AC = 2BD$ [From (1)] $2BD = 2s - 2b$ [as $AC = b$] $BD = s - b$</p>	
7.	<p>The radius of semicircle = $10/2 = 5 \text{ cm}$ Now, area of the region I +III = Area of square ABCD – Area of two semicircles of radius 5 cm $= (10)^2 - 2 \times (\frac{1}{2}) \pi \times (5)^2$ $= 100 - 3.14 \times 25$ $= 100 - 78.5$ $= 21.5 \text{ cm}^2$ Similarly, Area of the region II + Iv = 21.5 cm^2 Area of the shaded region = Area of square ABCD – Area of the region (I + II + III + IV)</p>	

$$\begin{aligned}
 &= 100 - 2 \times 21.5 \\
 &= 100 - 43 \\
 &= 57 \text{ cm}^2
 \end{aligned}$$

SECTION – D (5 MARKS QUESTIONS)

8. Volume of water in the overhead tank equals the volume of the water removed from the sump.
 Now, the volume of water in the overhead tank (cylinder) = $\pi r^2 h$
 $= 3.14 \times 0.6 \times 0.6 \times 0.95 \text{ m}^3$
 The volume of water in the sump when full = $l \times b \times h = 1.57 \times 1.44 \times 0.95 \text{ m}^3$
 The volume of water left in the sump after filling the tank
 $= [(1.57 \times 1.44 \times 0.95) - (3.14 \times 0.6 \times 0.6 \times 0.95)] \text{ m}^3 = (1.57 \times 0.6 \times 0.6 \times 0.95 \times 2) \text{ m}^3$
 Height of the water left in the sump = (volume of water left in the sump) / ($l \times b$)
 $= (1.57 \times 0.6 \times 0.6 \times 0.95 \times 2) / (1.57 \times 1.44)$
 $= 0.475 \text{ m}$
 $= 47.5 \text{ cm}$
 Capacity of tank / Capacity of sump = $(3.14 \times 0.6 \times 0.6 \times 0.95) / (1.57 \times 1.44 \times 0.95)$
 $= 1/2$
 Therefore, the capacity of the tank is half the capacity of the sump.

9. The dimension of $FH = EG = 14 - 3 - 3 = 14 - 6 = 8 \text{ cm}$
 The side of square JKLM will be 4 cm
 radius of the semicircle = $4/2 = 2 \text{ cm}$
 Area of the shaded region = area of square ABCD - area of square JKLM - area of 4 semicircles
 Area of square = (side)²
 Area of square ABCD = $(14)^2 = 196 \text{ cm}^2$
 Area of square JKLM = $(4)^2 = 16 \text{ cm}^2$
 Area of semicircle = $\pi r^2/2$
 Area of semicircle KEJ = $(22/7)(2)^2/2 = (22/7)(2) = 44/7 = 6.2857 \text{ cm}^2$
 Since all semicircles are equal.
 Area of 4 semicircle = $4(\text{area of one semicircle}) = 4(6.2857) = 25.14286 \text{ cm}^2$
 Area of the shaded region = $196 - 16 - 25.14286$
 $= 180 - 25.14286$
 $= 154.857 \text{ cm}^2$



SECTION – E (CASE STUDY)

10. a) Total surface area of boiler
 $= \text{SA of cylindrical part} + \text{SA of two hemisphere}$

$$= 6\pi r^2 + 2\left(\frac{4\pi r^2}{2}\right) = 6\pi r^2 + 4\pi r^2 = 10\pi r^2$$
- b) Volume of boiler,
 $= \text{Volume of cylinder} + \text{Volume of two hemisphere}$

$$= \pi r^2 l + 2\left(\frac{2\pi}{3} \times r^3\right) = \pi r^2 \cdot 3r + \frac{4\pi}{3} \times r^3 = \left(3 + \frac{4}{3}\right)\pi r^3 = \frac{13}{3}\pi r^3$$
- c) Ratio of volume to the surface = $\frac{\frac{13}{3}\pi r^3}{10\pi r^2} = \frac{13}{30}r$