

BCM SCHOOL BASANT AVENUE FUGRI ROAD LUDHIANA ASSIGNMENT OF CLASS XISC		
1	The value of $\tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ$ is (a) 0    (b) 1    (c) $\frac{1}{2}$ (d) Not defined Ans b	1
2	The value of $\frac{1 - \tan^2 15^\circ}{1 + \tan^2 15^\circ}$ is (a) 1    (b) $\sqrt{3}$ (c) $\frac{\sqrt{3}}{2}$ (d) 2 Ans c	1
3	The value of $\tan 75^\circ - \cot 75^\circ$ is equal to $\tan 75^\circ - \cot 75^\circ$  $\Rightarrow$ Now, $\tan 75^\circ = \tan (45^\circ + 30^\circ)$  $= \frac{\tan 45^\circ + \tan 30^\circ}{1 - \tan 45^\circ \tan 30^\circ} \left[ \because \tan (A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B} \right]$  $= \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}}$ $\Rightarrow \tan 75^\circ = \frac{\sqrt{3} + 1}{\sqrt{3} - 1} \quad \cot 75^\circ = \frac{1}{\tan 75^\circ} = \frac{\sqrt{3} - 1}{\sqrt{3} + 1}$  $\text{So, } \tan 75^\circ - \cot 75^\circ = \frac{\sqrt{3} + 1}{\sqrt{3} - 1} - \frac{\sqrt{3} - 1}{\sqrt{3} + 1}$  $= \frac{(\sqrt{3} + 1)^2 - (\sqrt{3} - 1)^2}{(\sqrt{3} - 1)(\sqrt{3} + 1)}$  $= \frac{3 + 1 + 2\sqrt{3} - 3 - 1 + 2\sqrt{3}}{3 - 1}$  $= \frac{4\sqrt{3}}{2} = 2\sqrt{3}$  <p style="text-align: center;"><b>OR</b></p> <p>Find the angle between the minute hand and hour hand of a clock when the time is 7:20.</p>	2

	<p>The correct option is <b>C</b> <math>100^\circ</math></p> <p><math>7 \text{ hr } 20 \text{ min} = 7 + \frac{20}{60} = \frac{22}{3} \text{ hr}</math></p> <p>Angle traced by hour hand in 7 hr 20 min = <math>\left(\frac{22}{3} \times \frac{360^\circ}{12}\right) = 220^\circ</math></p> <p>Angle traced by the minute hand in 20 min = <math>\left(\frac{360}{60} \times 20\right)^\circ = 120^\circ</math></p> <p>Hence, required angle between the two hands = <math>220^\circ - 120^\circ = 100^\circ</math></p>	
<b>4</b>	<p>The value of <math>\sin 50^\circ - \sin 70^\circ + \sin 10^\circ</math> is equal to</p> $\sin A - \sin B = 2 \cos \frac{A+B}{2} \sin \frac{A-B}{2}$ $\sin 50^\circ - \sin 70^\circ = 2 \cos \frac{50^\circ + 70^\circ}{2} \sin \frac{50^\circ - 70^\circ}{2} = -\sin 10^\circ$ <p><math>\therefore -\sin 10^\circ + \sin 10^\circ = 0</math></p>	<b>2</b>
<b>5</b>	<p>Prove that the value of <math>\sin 20^\circ \sin 40^\circ \sin 60^\circ \sin 80^\circ = \frac{3}{16}</math></p> $\begin{aligned} & \sin 20 \times \sin 40 \times \sin 60 \times \sin 80 \\ &= \sin 60 [\sin 20 \times \sin 40 \times \sin 80] \\ &= \frac{\sqrt{3}}{2} [\sin 20 \times \sin(60 - 20) \times \sin(60 + 20)] \\ &= \frac{\sqrt{3}}{2} [\sin 3(20)/4] \\ &= \frac{\sqrt{3}}{2} [\sin 60/4] \\ &= \frac{\sqrt{3}}{2} [\frac{\sqrt{3}}{2} \times 4] \\ &= \frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{8} \\ &= \frac{3}{16} \end{aligned}$	<b>2</b>
<b>6</b>	<p>Prove that</p> $\left(1 + \cos \frac{\pi}{8}\right) \left(1 + \cos \frac{3\pi}{8}\right) \left(1 + \cos \frac{5\pi}{8}\right) \left(1 + \cos \frac{7\pi}{8}\right) = \frac{1}{8}$	<b>3</b>

$$\begin{aligned}
\therefore \text{L.H.S.} &= \left(1 + \cos \frac{\pi}{8}\right) \left(1 + \cos \frac{3\pi}{8}\right) \cdot \left(1 - \cos \frac{3\pi}{8}\right) \left(1 - \cos \frac{\pi}{8}\right) \dots [\text{From (i) and (ii)}] \\
&= \left(1 - \cos^2 \frac{\pi}{8}\right) \left(1 - \cos^2 \frac{3\pi}{8}\right) \\
&= \sin^2 \frac{\pi}{8} \sin^2 \frac{3\pi}{8} \\
&= \frac{1}{4} \left(2 \sin \frac{\pi}{8} \sin \frac{3\pi}{8}\right)^2 \\
&= \frac{1}{4} \left[\cos\left(\frac{\pi}{8} - \frac{3\pi}{8}\right) - \cos\left(\frac{\pi}{8} + \frac{3\pi}{8}\right)\right]^2 \\
&= \frac{1}{4} \left[\cos\left(-\frac{\pi}{4}\right) - \cos\left(\frac{\pi}{2}\right)\right]^2 \\
&= \frac{1}{4} \left(\cos\left(\frac{\pi}{4}\right) - 0\right)^2 \\
&= \frac{1}{4} \left(\frac{1}{\sqrt{2}}\right)^2 \\
&= \frac{1}{4} \left(\frac{1}{2}\right) \\
&= \frac{1}{8}
\end{aligned}$$

**7** Sketch the graph of  $y = \sin x$  and  $\sin 2x$  on the same scale

**4**

