|  | ANSWER KEY CLASS XII MATHS |  |
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| 1 | A |  |
| 2 | C |  |
| 3 | Set A is the set of all books in the library of a college. <br> $R=\{(x, y): x$ and $y$ have the same number of pages $\}$ <br> Now, $R$ is reflexive since $(x, x) \in R$ as $x$ and $x$ has the same number of pages. <br> Let $(x, y) \in R \Rightarrow x$ and $y$ have the same number of pages. <br> $\Rightarrow y$ and $x$ have the same number of pages. $\Rightarrow(\mathrm{y}, \mathrm{x}) \in \mathrm{R}$ <br> $\therefore \mathrm{R}$ is symmetric. <br> Now, let $(\mathrm{x}, \mathrm{y}) \in \mathrm{R}$ and $(\mathrm{y}, \mathrm{z}) \in \mathrm{R}$ <br> $\Rightarrow x$ and $y$ and have the same number of pages and $y$ and $z$ have the same number of pages. <br> $\Rightarrow \mathrm{x}$ and z have the same numbers of pages. $\Rightarrow(\mathrm{x}, \mathrm{z}) \in \mathrm{R}$ <br> $\therefore \mathrm{R}$ is transitive. <br> Hence, R is an equivalence relation. |  |
| 4 | $R$ is an equivalance relation if $R$ is reflexive,symmetric and transitive. <br> a)checking if it is reflexive; <br> Given R in A $\times$ Aand $(\mathrm{a}, \mathrm{b}) \mathrm{R}(\mathrm{c}, \mathrm{d})$ suchthata+d=b+c <br> For reflexive,consider $(\mathrm{a}, \mathrm{b}) \mathrm{R}(\mathrm{a}, \mathrm{b})(\mathrm{a}, \mathrm{b}) \in \mathrm{A}$ <br> and applying given condition $\Rightarrow \mathrm{a}+\mathrm{b}=\mathrm{b}+\mathrm{a}$; which is true for all A <br> $\therefore$ Risreflexive. <br> b)checking if it is symmetric; <br> given $(a, b) R(c, d)$ suchthata $+d=b+c$ |  |


|  | consider (c, d) $\mathrm{R}(\mathrm{a}, \mathrm{b}) \mathrm{onA} \times \mathrm{A}$ <br> applying given condition $\Rightarrow c+b=d+a w h i c h s a t i s f i e s g i v e n c o n d i t i o n ~$ <br> Hence R is symmetric. <br> c)checking if it is transitive; <br> $\operatorname{Let}(\mathrm{a}, \mathrm{b}) \mathrm{R}(\mathrm{c}, \mathrm{d}) \operatorname{and}(\mathrm{c}, \mathrm{d}) \mathrm{R}(\mathrm{e}, \mathrm{f})$ <br> $\operatorname{and}(\mathrm{a}, \mathrm{b}),(\mathrm{c}, \mathrm{d}),(\mathrm{e}, \mathrm{f}) \in \mathrm{A} \times \mathrm{A}$ <br> applying given condition: $\Rightarrow \mathrm{a}+\mathrm{d}=\mathrm{b}+\mathrm{c} \rightarrow 1$ andc $+\mathrm{f}=\mathrm{d}+\mathrm{e} \rightarrow 2$ <br> equation $1 \Rightarrow a-c=b-d$ <br> nowaddequation1and2; <br> $\Rightarrow \mathrm{a}-\mathrm{c}+\mathrm{c}+\mathrm{f}=\mathrm{b}-\mathrm{d}+\mathrm{d}+\mathrm{e}$ <br> $\Rightarrow \mathrm{a}+\mathrm{f}=\mathrm{b}+\mathrm{e}$ <br> $\therefore(\mathrm{a}, \mathrm{b}) \mathrm{R}(\mathrm{e}, \mathrm{f})$ also satisfies the condition <br> Hence R is transitive. |
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| 5 | We have $g o f(x)=g((3 x+4) /(5 x-7))=(7((3 x+4) /(5 x-7))+$ <br> $4) /(5((7 x+4) /(5 x-7))-3)=(21 x+28+20 x-28) /(15 x+20-$ $15 x+21)=41 x / 41=x$ <br> Similarly, $f \circ g(x)=f((7 x+4) /(5 x-3))=(3(7 x+4) /(5 x-3))+4) /(5(7 x+$ <br> 4) $/(5 x-3))-7)=(21 x+12+20 x-12) /(35 x+20-35 x+21)=$ $41 x / 41=x$ <br> Thus, gof $(x)=x, \forall x \in B$ and fog $(x)=x, \forall x \in A$, which implies that gof = IB and fog = IA. |

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\(6 \quad\) We have, the function \(f: R \rightarrow R\) defined by
\(f(x)=\frac{x}{x^{2}+1} \forall x \in R\)
For one-one:
Let \(x_{1}, x_{2} \in R\)
Now,
\(f\left(x_{1}\right)=f\left(x_{2}\right)\)
\(\Rightarrow \frac{x_{1}}{x_{1}^{2}+1}=\frac{x_{2}}{x_{2}^{2}+1}\)
\(\Rightarrow x_{1} x_{2}^{2}+x_{1}=x_{2} x_{1}^{2}+x_{2}\)
\(\Rightarrow x_{1} x_{2}^{2}-x_{2} x_{1}^{2}+x_{1}-x_{2}=0\)
\(\Rightarrow-x_{1} x_{2}\left[x_{1}-x_{2}\right]+\left(x_{1}-x_{2}\right)=0\)
\(\Rightarrow\left(x_{1}-x_{2}\right)\left(1-x_{1} x_{2}\right)=0\)
\(\Rightarrow x_{1}=x_{2}\) or \(x_{1} x_{2}=1\)
\(\Rightarrow x_{1}=x_{2}\) or \(x_{1} x_{2}=1\)
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But, there exists some values of $x_{1}$ and $x_{2}$ so that $x_{1} \neq x_{2}$ but $f\left(x_{1}\right)=f\left(x_{2}\right)$

Like $x_{1}=2$ and $x_{2}=\frac{1}{2}$ then,
$f\left(x_{1}\right)=\frac{2}{5}$ and $f\left(x_{2}\right)=\frac{2}{5}$ but $x_{1} \neq x_{2}$

Hence, $f(x)$ is not one-one.

For onto:
Again, consider a value ' 1 ' as element in co-domain $R$.
$\Rightarrow \frac{x}{x^{2}+1}=1$
$\Rightarrow x^{2}+1=x$

|  | i.e., quadratic equation in x |
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| Here, discriminant D < 0. |  |
| Hnece, there is no real value of $\mathrm{x} \in \mathrm{R}$ for which $\mathrm{f}(\mathrm{x})=1$. |  |
| $\therefore \mathrm{f}$ is not an onto function. |  |
| Thus, f is neither one-one nor onto. |  |

