

	ANSWER KEY XISC	
1	D	
2	A	
3	<p>(i) $n(A) = n(A - B) + n(A \cap B)$ $= 14 + x + x$ $= 14 + 2x$</p> <p>$n(B) = n(B - A) + n(A \cap B)$ $= 3x + x$ $= 4x$</p> <p>but $n(A) = n(B)$ (Given) $14 + 2x = 4x$ $x = 7$</p> <p>(ii) $n(A \cup B) = n(A - B) + n(B - A) + n(A \cap B)$ $= 14 + x + 3x + x$ $= 14 + 5x = 14 + 5 \times 7 = 49$</p>	
4	<p>$C - B = A$ $= (A \cup B) - B$ $= (A \cup B) \cap B'$ $= B' \cap (A \cup B)$ $= (B' \cap A) \cup (B' \cap B)$ $= (B' \cap A) \cup \phi$ $= B' \cap A$ $= A \cap B'$ $= A - B$ $= A$ (Proved) $[\because A \cap B = \phi]$</p>	

	<p style="text-align: center;">OR</p> <p>Let $x \in A \cup B$ $\Rightarrow x \in A$ or $x \in B$ $\Rightarrow x \in B \quad \{ \because A \subset B \}$ $\Rightarrow A \cup B \subset B \dots(1)$ We know that, $B \subset A \cup B$ {this is always true} $\dots(2)$ From (1) and (2) $A \cup B = B$ Now, suppose $y \in A$ $\Rightarrow y \in A \cup B$ $\Rightarrow y \in B \quad \{ \because A \cup B = B \}$ $\Rightarrow A \subset B$ Therefore, $A \subset B \Leftrightarrow A \cup B = B$ Hence Proved</p>	
5	<p>For $Df, f(x)$ must be real number $\Rightarrow 3x^2 - 5$ must be a real number Which is a real number for every $x \in R$ $\Rightarrow Df = R \dots\dots\dots(i)$ for Rf, let $y = f(x) = 3x^2 - 5$ We know that for all $x \in R, x^2 \geq 0 \Rightarrow 3x^2 \geq 0$ $\Rightarrow 3x^2 - 5 \geq -5 \Rightarrow y \geq -5 \Rightarrow Rf = [-5, \infty]$ Further, as $-3 \in Df, f(-3)$ exists is and $f(-3)$ $= 3(-3)^2 - 5 = 22$. As $43 \in Rf$ on putting $y = 43$ is (i) we get $3x^2 - 5 = 43 \Rightarrow 3x^2 = 48 \Rightarrow x^2 = 16 \Rightarrow x = -4, 4$. Therefore -4 and 4 are number (is Df) which are associated with the number 43 in Rf</p>	
6	<p>For $Df, f(x)$ must be a real number $\Rightarrow \sqrt{x^2 - 4}$ Must be a real number $\Rightarrow x^2 - 4 \geq 0 \Rightarrow (x+2)(x-2) \geq 0$ \Rightarrow either $x \leq -2$ or $x \geq 2$ $\Rightarrow D_f = (-\infty, -2] \cup [2, \infty)$.</p>	

For R_f , let $y = \sqrt{x^2 - 4}$(i)

As square root of a real number is always non-negative, $y \geq 0$

On squaring (i), we get $y^2 = x^2 - 4$

$\Rightarrow x^2 = y^2 + 4$ but $x^2 \geq 0$ for all $x \in D_f$

$\Rightarrow y^2 + 4 \geq 0 \Rightarrow y^2 \geq -4$, which is true for all $y \in R$.

also $y \geq 0$

$\Rightarrow R_f = [0, \infty)$

OR

For D_f , $f(x)$ must be a real no.

$\Rightarrow |x+2| \neq 0 \Rightarrow x+2 \neq 0 \Rightarrow x \neq -2$

\therefore **Domain of f = set of all real numbers**

except -2 i.e. $D_f = R - \{-2\}$

for R_f

case I if $x+2 > 0$ then $|x+2| = x+2$

$$\therefore f(x) = \frac{x+2}{|x+2|} = 1$$

case II if $x+2 < 0$, $|x+2| = -(x+2)$

$$\therefore f(x) = \left(\frac{x+2}{-x-2} \right) = -1$$

\therefore Range of $f = \{-1, 1\}$

7 Let A and B be two sets having m and n elements respectively

no of subsets of A = 2^m

no of subsets of B = 2^n

According to question

$$\mathbf{2^m = 56 + 2^n}$$

$$\mathbf{2^m - 2^n = 56}$$

$$2^n (2^{m-n} - 1) = 56$$

$$2^n (2^{m-n} - 1) = 2^3 (2^3 - 1)$$

$$2^n = 2^3$$

$$n = 3$$

$$m - n = 3$$

$$m - 3 = 3$$

$$m = 6$$