

BCM SCHOOL, BASANT AVENUE, DUGRI ROAD, LUDHIANA
Class XI (Trigonometric functions)

Sol	(c)
1.	Range of $\sin \theta$, $\cos \theta = [-1, 1]$ and $\sec \theta = \frac{1}{\cos \theta}$. So, $ \sec \theta \geq 1$. Identify which violates.
2.	(b) Convert $1 \text{ rad} = \frac{180^\circ}{\pi} \approx 57^\circ$. Compare 1° and 1 radian
3.	(d) Use identity of $\sin 2x$ and maximum value of sine function is 1.
4.	Range: $(-\infty, -1] \cup [1/3, \infty)$ We know, $\cos x \in [-1, 1]$. Using it, find range of $1-2\cos x$, then take reciprocal carefully. Exclude denominator = 0.
5.	General solution: $x = -\pi/4 + n\pi$ $1 + \tan x = 0 \Rightarrow \tan x = -1$. Use general solution of $\tan x$.
6.	$\tan 2\alpha = 56/33$ $\cos(\alpha + \beta) = \frac{4}{5}$, So $\sin(\alpha + \beta) = \frac{3}{5} \Rightarrow \tan(\alpha + \beta) = \frac{3}{4}$ And $\sin(\alpha - \beta) = \frac{5}{13}$, so $\cos(\alpha - \beta) = \frac{12}{13} \Rightarrow \tan(\alpha - \beta) = \frac{5}{12}$ Now, $\tan 2\alpha = \tan((\alpha + \beta) + (\alpha - \beta))$ $\tan 2\alpha = \frac{\tan(\alpha + \beta) + \tan(\alpha - \beta)}{1 - \tan(\alpha + \beta) \tan(\alpha - \beta)} = \frac{\frac{3}{4} + \frac{5}{12}}{1 - \frac{3}{4} \cdot \frac{5}{12}} = \frac{56}{33}$
7.	$\frac{1}{8}$ $\cos \frac{7\pi}{8} = \cos(\pi - \frac{\pi}{8}) = -\cos \frac{\pi}{8}$ and $\cos \frac{5\pi}{8} = \cos(\pi - \frac{3\pi}{8}) = -\cos \frac{3\pi}{8}$ So, we have $(1 - \cos^2 \frac{\pi}{8})(1 - \cos^2 \frac{3\pi}{8}) = \sin^2 \frac{\pi}{8} \sin^2 \frac{3\pi}{8}$ $\Rightarrow \frac{1}{4} (2 \sin \frac{\pi}{8} \sin \frac{3\pi}{8})^2 = \frac{1}{8}$ (By using product to sum identity)
8.	$\frac{3}{2}$ Use $\cos^2 x = (1 + \cos 2x)/2$ to get $\frac{1}{2} [1 + \cos 2x + 1 + \cos(2x + \pi/3) + 1 + \cos(2x - 2\pi/3)]$ $= \frac{1}{2} [3 + \cos 2x + 2 \cos 2x \cos \frac{2\pi}{3}]$ (By using sum to product identity) $= \frac{1}{2} [3 + \cos 2x - \cos 2x] = \frac{3}{2}$
9.	On dividing and multiplying by $2 \sin \pi/7$, $= \frac{1}{2 \sin \frac{\pi}{7}} (\sin \frac{2\pi}{7} \cos \frac{2\pi}{7} \cos \frac{4\pi}{7}) = \frac{1}{4 \sin \frac{\pi}{7}} (\sin \frac{4\pi}{7} \cos \frac{4\pi}{7}) = \frac{1}{8 \sin \frac{\pi}{7}} (\sin \frac{8\pi}{7})$ $= \frac{1}{8 \sin \frac{\pi}{7}} (\sin(\pi + \pi/7)) = -\frac{1 \sin \frac{\pi}{7}}{8 \sin \frac{\pi}{7}} = -\frac{1}{8}$
10.	(i) 2 points (ii) 2 points (iii) 4 points Solve $\sin x = \cos x \Rightarrow \tan x = 1$. Count solutions in $[-2\pi, 2\pi]$. OR 2 points Check if $\sin x = \sqrt{2}$ is possible using range of sine function.