

BCM SCHOOL, BASANT AVENUE, DUGRI, LUDHIANA.
SEPTEMBER ASSIGNMENT
CLASS- X (MATHEMATICS)

SECTION -A (MULTIPLE CHOICE QUESTIONS)

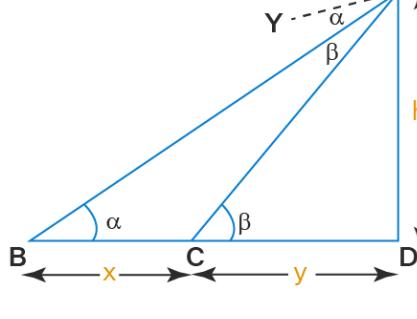
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| 1. | a |
| 2. | c |
| 3. | b |
| 4. | d |

SECTION B(2 MARKS QUESTIONS)

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| 5. | Mode = 65.625 |
| 6. | <p>Let $P(x,y)$, $Q(a+b,b-a)$ and $R(a-b,a+b)$ be the given points. Then, $PQ=PR$</p> $\Rightarrow \sqrt{(x-(a+b))^2 + (y-(b-a))^2} = \sqrt{(x-(a-b))^2 + (y-(a+b))^2}$ $\Rightarrow (x-(a+b))^2 + (y-(b-a))^2 = (x-(a-b))^2 + (y-(a+b))^2$ $\Rightarrow x^2 - 2x(a+b) + (a+b)^2 + y^2 - 2y(b-a) + (b-a)^2$ $= x^2 + (a-b)^2 - 2x(a-b) + y^2 - 2y(a+b) + (a+b)^2$ $\Rightarrow -2x(a+b) - 2y(b-a) = -2x(a-b) - 2y(a+b)$ $\Rightarrow ax + bx + by - ay = ax - bx + ay + by$ $\Rightarrow 2bx = 2ay \Rightarrow bx = ay$ |
| 7. | <p>(A) $44/52 = 11/13$
 (B) $20/52 = 5/13$.
 (C) $16/52 = 4/13$.
 (D) $13/52 = 1/4$
 (E) $1/52$.</p> |

SECTION – C (3 MARKS QUESTIONS)

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| 8. | <p>In ΔOPQ, we have</p> $OQ^2 = OP^2 + PQ^2$ $\Rightarrow (PQ + 1)^2 = OP^2 + PQ^2 [\because OQ - PQ = 1 \Rightarrow OQ = 1 + PQ]$ $\Rightarrow PQ^2 + 2PQ + 1 = OP^2 + PQ^2$ $\Rightarrow 2PQ + 1 = 49$ $\Rightarrow PQ = 24 \text{ cm}$ $\therefore OQ - PQ = 1 \text{ cm}$ $\Rightarrow OQ = (PQ + 1)\text{cm} = 25 \text{ cm}$ <p>Now, $\sin Q = \frac{OP}{OQ} = \frac{7}{25}$
 and, $\cos Q = \frac{PQ}{OQ} = \frac{24}{25}$</p> |
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9.	<p>Distance between (0, 0) and (x, y) = Distance between (0, 0) and (3, $\sqrt{3}$) = Distance between (x, y) and (3, $\sqrt{3}$)</p> $\sqrt{x^2 + y^2} = \sqrt{(3^2 + 3)} = \sqrt{(x - 3)^2 + (y - \sqrt{3})^2}$ $x^2 + y^2 = 12$ $x^2 + 9 - 6x + y^2 + 3 - 2\sqrt{3}y = 12$ <p>On solving, $x = \frac{6-\sqrt{3}y}{3}$ and $y = 2\sqrt{3}$ or $-\sqrt{3}$ So, the third vertex of the equilateral triangle = $(0, 2\sqrt{3})$ or $(3, -\sqrt{3})$.</p>
10.	$\begin{aligned} \text{LHS} &= 2(\sin^6 \theta + \cos^6 \theta) - 3(\sin^4 \theta + \cos^4 \theta) + 1 \\ &= 2\{(\sin^2 \theta + \cos^2 \theta)^3 - 3 \sin^2 \theta \cos^2 \theta (\sin^2 \theta + \cos^2 \theta)\} - 3(\sin^2 \theta + \cos^2 \theta)^2 \end{aligned}$ <p>We know, $[\sin^2 x + \cos^2 x = 1]$</p> $\begin{aligned} &= 2\{1 - 3 \sin^2 \theta \cos^2 \theta\} - 3\{1 - 2 \sin^2 \theta \cos^2 \theta\} + 1 \\ &= 2 - 6 \sin^2 \theta \cos^2 \theta - 3 + 6 \sin^2 \theta \cos^2 \theta + 1 \\ &= 0 \end{aligned}$
SECTION – D (5 MARKS QUESTIONS)	
11.	<p>Considering triangle ABD, we get</p> $\tan \alpha = AD/BD$ $\tan \alpha = h/BC + CD$ $\tan \alpha = h/x+y$ $y = h/\tan \alpha - x \quad \dots \dots \dots (1)$ <p>Considering triangle ACD, we get</p> $\tan \beta = AD/CD$ $\tan \beta = h/y$ $y = h/\tan \beta \quad \dots \dots \dots (2)$ <p>Now, by comparing (1) and (2), we get,</p> $h/\tan \alpha - x = h/\tan \beta$ $x = h/\tan \alpha - h/\tan \beta$ $x = h(1/\tan \alpha - 1/\tan \beta)$ $x = h(\cot \alpha - \cot \beta)$ <p>Therefore, the required distance is $h(\cot \alpha - \cot \beta)$.</p> 

12.	<p>$\therefore PT = ST = x$</p> <p>Thus, in right triangle PQT, we have</p> <p>$QT = 27 - x$, $PT = x$ and $PQ = 9$</p> <p>Using Pythagoras theorem, we have</p> $PT^2 = PQ^2 + QT^2 \Rightarrow x^2 = 9^2 + (27 - x)^2$ $\Rightarrow x^2 = 81 + 729 - 54x + x^2 \Rightarrow 0 = 810 - 54x \Rightarrow 54x = 810 \Rightarrow x = 15$ $\therefore QT = SQ - ST = (27 - 15)m = 12m$ <p>Hence the snake is caught at a distance of 12m from the hole.</p>	
13.	<p>Let the four consecutive numbers in AP be $(a - 3d)$, $(a - d)$, $(a + d)$ and $(a + 3d)$</p> <p>So, according to the question.</p> $a - 3d + a - d + a + d + a + 3d = 32$ <p>On solving $a = 8$</p> <p>Now, $(a - 3d)(a + 3d)/(a - d)(a + d) = 7/15$</p> $15(a^2 - 9d^2) = 7(a^2 - d^2)$ $15a^2 - 135d^2 = 7a^2 - 7d^2$ $15a^2 - 7a^2 = 135d^2 - 7d^2$ $8a^2 = 128d^2$ <p>Putting the value of $a = 8$ in above we get.</p> $8(8)^2 = 128d^2$ $128d^2 = 512$ $d^2 = 512/128$ $d^2 = 4$ <p>On solving, $d = \pm 2$</p> <p>Four consecutive numbers are 2, 6, 10 and 14</p>	
SECTION – E (CASE STUDY)		
14.	<p>a) length = x, breadth = $x-3$ b) $x^2 - 9x + 14 = 0$ c) length = 7m and breadth = 4m OR Area of triangular part = $24 m^2$</p>	
15.	<p>a) 3900 b) 73500 c) 4900 OR 10:49</p>	