

BCM SCHOOL BASANT AVENUE DUGRI ROAD LUDHIANA
 ASSIGNMENT OF BINOMIAL THEOREM
 XI SC
 ANSWER KEY (MATHS)

ANSWER KEY CLASS XI SC

- 1 c
 2 b
 3 c

4 Given that, a_1, a_2, \dots, a_n are in A.P., $\forall a_i > 0$
 $\therefore a_1 - a_2 = a_2 - a_3 = \dots = a_{n-1} - a_n = -d$ (constant) (1)

Now,
$$\frac{1}{\sqrt{a_1} + \sqrt{a_2}} + \frac{1}{\sqrt{a_2} + \sqrt{a_3}} + \dots + \frac{1}{\sqrt{a_{n-1}} + \sqrt{a_n}}$$

$$= \frac{\sqrt{a_1} - \sqrt{a_2}}{a_1 - a_2} + \frac{\sqrt{a_2} - \sqrt{a_3}}{a_2 - a_3} + \dots + \frac{\sqrt{a_{n-1}} - \sqrt{a_n}}{a_{n-1} - a_n}$$
 (rationalizing)

$$= \frac{\sqrt{a_1} - \sqrt{a_2}}{-d} + \frac{\sqrt{a_2} - \sqrt{a_3}}{-d} + \dots + \frac{\sqrt{a_{n-1}} - \sqrt{a_n}}{-d}$$

$$= \frac{1}{-d} [\sqrt{a_1} - \sqrt{a_n}]$$

$$= \frac{a_1 - a_n}{-d(\sqrt{a_1} + \sqrt{a_n})}$$
 (rationalizing)

$$= \frac{-(n-1)d}{-d(\sqrt{a_1} + \sqrt{a_n})}$$
 (as $a_n = a_1 + (n-1)d$)

$$= \frac{n-1}{\sqrt{a_1} + \sqrt{a_n}}$$

5 It has to be proved that the sequence: $aA, arAR, ar^2AR^2, \dots, ar^{n-1}AR^{n-1}$, forms a G.P.

$$\frac{\text{Second term}}{\text{First term}} = \frac{arAR}{aA} = rR$$

$$\frac{\text{Third term}}{\text{Second term}} = \frac{ar^2AR^2}{arAR} = rR$$

Thus, the above sequence forms a G.P. and the common ratio is rR .

6 The coeff. Of the first three terms of $\left(x - \frac{3}{x^2}\right)^m$ are ${}^m C_0, (-3)^m {}^m C_1$ and

$$9 \binom{m}{2}$$

Therefore, by the given condition

$$\binom{m}{0} - 3 \binom{m}{1} + 9 \binom{m}{2} = 559$$

$$1 - 3m + \frac{9m(m-1)}{2} = 559$$

On solving we get $m = 12$

$$\begin{aligned} T_{r+1} &= \binom{12}{r} (x)^{12-r} \left(\frac{-3}{x^2}\right)^r \\ &= \binom{12}{r} (x)^{12-r} \cdot (-3)^r \cdot (x)^{-2r} \\ &= \binom{12}{r} (x)^{12-3r} \cdot (-3)^r \end{aligned}$$

$$12 - 3r = 3 \Rightarrow r = 3, \text{ req. term is } -5940 x^3$$

7 **a = 3, b = 2, n=3**

8

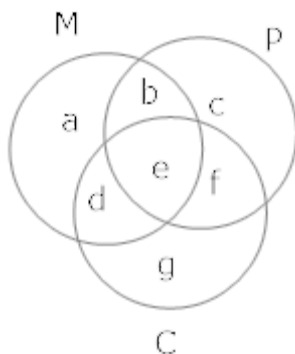
9 (i) $n(H \cup S) = n(H) + n(S) - n(H \cap S)$
 $= 30 + 25 - 16$
 $= 39$

(ii) $n(H' \cap S') = n(H \cup S)'$
 $= n(U) - n(H \cup S)$
 $= 50 - 39 = 11$

(iii) $n(H \cup S) = n(H) + n(S) - 2n(H \cap S)$
 $= 30 + 25 - 2 \times 16$
 $= 23$

1 $n(M) = a + b + d + e = 15$

0



$$n(P) = b + c + e + f = 12$$

$$n(C) = d + e + f + g = 11$$

$$n(M \cap P) = b + e = 9$$

$$n(M \cap C) = d + e = 5$$

$$n(P \cap C) = e + f = 4$$



$$e = 3$$

$$\text{so } b = 6, d = 2, f = 1$$

$$a = 4, g = 5, c = 2$$

$$(i) g = 5,$$

$$(ii) a = 4,$$

$$(iii) c = 2$$

$$(iv) f = 1,$$

$$(v) b = 6,$$

$$(vi) g + a + c = 11$$

$$(vii) a + b + c + d + e + f + g = 23$$

$$(viii) 25 - (a + b + c + d + e + f + g) = 25 - 23 = 2$$

