

**BCM SCHOOL, BASANT AVENUE, DUGRI, LUDHIANA.**  
**DECEMBER ASSIGNMENT ANSWER KEY / HINTS (2025-26)**  
**CLASS- IX (MATHEMATICS)**  
**TOPIC: CIRCLES**

**SECTION –A (MULTIPLE CHOICE QUESTIONS)**

1.	(d) $150^\circ$
2.	(c) $45^\circ$
3.	(a)
5.	$\angle AOB = 80^\circ$ , $\angle OAB = 50^\circ$
6.	<p>Let ABC be the triangle whose circumcenter is O.          So, <math>OB = OC</math>  <math>\angle OBC = \angle OCB = \theta</math> (opposite angles of equal sides)          In <math>\triangle BOC</math>, using the angle sum property of triangle, sum of all angles is <math>180^\circ</math>, we have:  <math>\angle BOC + \angle OBC + \angle OCB = 180^\circ</math>  <math>\Rightarrow \angle BOC + \theta + \theta = 180^\circ</math>  <math>\Rightarrow \angle BOC = 180^\circ - 2\theta</math>          Also, in a circle, angle subtended by an arc at the center is twice the angle subtended by it at any other point in the remaining part of the circle.  <math>\angle BOC = 2\angle BAC</math>  <math>\Rightarrow \angle BAC = \frac{1}{2}(\angle BOC)</math>  <math>\Rightarrow \angle BAC = \frac{1}{2}(180^\circ - 2\theta)</math>  <math>\Rightarrow \angle BAC = (90^\circ - \theta)</math>  <math>\Rightarrow \angle BAC + \theta = 90^\circ</math>  <math>\Rightarrow \angle BAC + \angle OBC = 90^\circ</math>          Hence proved.</p>
9.	<p>Given: <math>y = 32^\circ</math> and <math>z = 40^\circ</math>          Proof: Let the line segments AD and CE cut each other at P.          Since,  <math>\angle APE = \angle CPD</math> [Vertically opposite angles]          Therefore, <math>\angle APE = x</math>          Now, <math>\angle BCP = \angle CDP + \angle CPD</math> [Exterior angle]          And <math>\angle PAB = \angle PEA + \angle APE</math> [Exterior angle]  <math>\angle BCP = x + y</math> ...(i)          and <math>\angle PAB = x + z</math> ...(ii)          Since ABCP is a cyclic quadrilateral,  <math>\angle BCP + \angle PAB = 180^\circ</math>  <math>\Rightarrow x + y + x + z = 180^\circ</math></p>

$$2x + (y + z) = 180^\circ \quad \dots(iii)$$

$$2x + (40^\circ + 32^\circ) = 180^\circ$$

$$2x = 180 - 72^\circ$$

$$\Rightarrow 2x = 108^\circ \Rightarrow x = 54^\circ$$

Since from (iii), we get

$$2x + (y + z) = 180^\circ$$

and

$$y + z = 90^\circ \quad [\text{Given}]$$

Therefore,

$$2x + 90^\circ = 180^\circ \Rightarrow 2x = 90^\circ$$

Therefore,

$$x = 45^\circ$$