

**BCM SCHOOL, BASANT AVENUE, DUGRI, LUDHIANA.  
OCTOBER ASSIGNMENT- ANSWER KEY  
CLASS- IX (MATHEMATICS)  
TOPICS: QUADRILATERALS & CIRCLES.**

**SECTION –A (MULTIPLE CHOICE QUESTIONS)**

1. d) Opposite angles are bisected by the diagonals

2. c)  $50^\circ$

3. d)  $45^\circ$

**SECTION B( 2 MARKS QUESTIONS)**

4.  $50^\circ$

5.  $175^\circ$

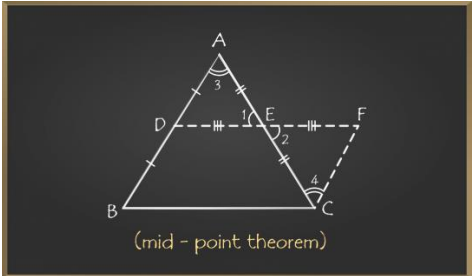
**SECTION – C (3 MARKS QUESTIONS)**

6.  $\angle DAB = 2x$   
 $\angle DCB = 2y$   
 We know that opposite angles of a parallelogram are equal.  
 So,  $\angle A = \angle C$   
 $2x = 2y$   
 $x = y$   
 As  $DC \parallel AB$ ,  $XC \parallel AY$   
 $\angle XCY = \angle CYB$  [Alternate angles]  
 $\angle CYB = x$   
 $\angle XAY = x$   
 As  $\angle XAY$  and  $\angle CYB$  are corresponding angles  
 $AX \parallel CY$   
 Therefore, AX is parallel to CY.

7.  $\therefore \angle BOC = \angle BCO$   
 | Angles opposite to equal sides of a triangle are equal  
 $\Rightarrow \angle BOC = y \dots(1)$   
 In  $\triangle BOC$ ,  
 $\angle OBA = \angle BOC + \angle BCO$   
 |  $\therefore$  An exterior angle of a triangle is equal to the sum of its two interior opposite angles  
 $= y + y$   
 $= 2y \dots(2)$   
 In  $\triangle OAB$ ,  
 $\therefore OA = OB$   
 | Radii of the same circle  
 $\Rightarrow \angle OAB = \angle OBA$   
 | Angles opposite to equal sides of a triangle are equal  
 $\Rightarrow \angle OAB = 2y \dots(3)$   
 Now,  $\therefore$  DOC is a straight line  
 $\therefore \angle AOD + \angle AOB + \angle BOC = 180^\circ$   
 $\Rightarrow x + \{180^\circ - (\angle OAB + \angle OBA)\} + y = 180^\circ$   
 | Angle sum property of a triangle  
 $\Rightarrow x + 180^\circ - (2y + 2y) + y = 180^\circ$   
 $\Rightarrow x = 3y$

**SECTION – D (5 MARKS QUESTIONS)**

8.  $\triangle AED \cong \triangle CEF$  by SAS criteria  
 $\angle 3 = \angle 4$  (c.p.c.t)  
 But these are alternate interior angles.  
 So,  $AB \parallel CF$   
 $AD = CF$  (c.p.c.t)  
 But  $AD = DB$  (D is the mid-point)  
 Therefore,  $BD = CF$   
 In BCFD  
 $BD \parallel CF$  (as  $AB \parallel CF$ )  
 $BD = CF$   
 BCFD is a parallelogram as one pair of opposite sides is parallel and equal.  
 Therefore,  $DF \parallel BC$  (opposite sides of parallelogram)  
 $DF = BC$  (opposite sides of parallelogram)  
 As  $DF \parallel BC$ ,  $DE \parallel BC$  and  $DF = BC$   
 But  $DE = EF$   
 So,  $DF = 2(DE)$   
 $2(DE) = BC$   
 $DE = \frac{1}{2}(BC)$



9. Proof:  $\angle XPY = 2\angle XZY$  ... (1)  
 | The angle subtended by an arc of a circle at the centre is twice the angle subtended by it at any point on the remaining part of the circle  
 $\angle YPZ = 2\angle YXZ$  ... (2)  
 | The angle subtended by an arc of a circle at the centre is twice the angle subtended by it at any point on the remaining part of the circle  
 Adding (1) and (2), we get,  
 $\angle XPY + \angle YPZ = 2\angle XZY + 2\angle YXZ$   
 $\Rightarrow \angle XPZ = 2(\angle XZY + \angle YXZ)$   
 $\Rightarrow 2(\angle XZY + \angle YXZ) = \angle XPZ.$

**SECTION – E (CASE STUDY)**

10. 1. In  $\triangle BIA$  and  $\triangle BIC$ ,

$\angle ABI = \angle CBI$  [BD is a bisector of angle B]  
 $BI = BI$  [Common]  
 $\angle BIA = \angle BIC$  [Each 90°]  
 $\therefore \triangle BIA \cong \triangle BIC$  [SAS congruence rule]  
 $\therefore AI = CI$  [CPCT]

It means  $I$  is the mid-point of  $AC$ . Hence proved

2. Here,  $HG = \frac{1}{2}AC$  [By mid-point theorem] and  
 $EF = \frac{1}{2}AC$  [By mid-point theorem]  
 $GH \parallel EF$  and  $HG = EF$   
 If in a quadrilateral opposite side is parallel and equal then the quadrilateral is a parallelogram. So, quadrilateral EFGH is a parallelogram.

3. It is false, because every parallelogram is not a rectangle.